

Harnack Inequalities for Non–Negative Solutions to Degenerate and Singular Parabolic Partial Differential Equations

Ugo Gianazza

Dipartimento di Matematica “F. Casorati”, Università di Pavia
via Ferrata 1, 27100 Pavia, Italy – email: gianazza@imati.cnr.it

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